

## Algebra of Matrices

### Transpose of matrix

ex:  $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}_{2 \times 3}$

- Interchanging row by column
- Transpose of any matrix is always denoted by,  $A^T = \begin{bmatrix} 1 & 4 \\ 2 & 5 \\ 3 & 6 \end{bmatrix}_{3 \times 2}$

Symmetric matrix  
 $A = A^T$

Skew-symmetric matrix  
 $A = -A^T$

### Addition or Substrac<sup>n</sup> of two matrix

it happens only if the order of two matrices are equal

$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}_{2 \times 3}$   $B = \begin{bmatrix} 0 & -1 & 3 \\ 2 & 1 & -4 \end{bmatrix}_{2 \times 3}$

$A+B = \begin{bmatrix} 1+0 & 2+(-1) & 3+3 \\ 4+2 & 5+1 & 6+(-4) \end{bmatrix}$

$A+B = \begin{bmatrix} 1 & 1 & 6 \\ 6 & 6 & 2 \end{bmatrix}_{2 \times 3}$

$A-B = \begin{bmatrix} 1-0 & 2-(-1) & 3-3 \\ 4-2 & 5-1 & 6-(-4) \end{bmatrix}$

$= \begin{bmatrix} 1 & 3 & 0 \\ 2 & 4 & 10 \end{bmatrix}_{2 \times 3}$

### Scalar multiplication

eg =  $A = \begin{bmatrix} 1 & 2 \\ 4 & 3 \end{bmatrix}_{2 \times 2}$

Find  $4A = 4 \begin{bmatrix} 1 & 2 \\ 4 & 3 \end{bmatrix} = \begin{bmatrix} 4 & 8 \\ 16 & 12 \end{bmatrix}$

$A = \begin{bmatrix} 1 & 2 \\ 4 & 5 \end{bmatrix}$   
 $= \begin{bmatrix} 1g & 2g \\ 4g & 5g \end{bmatrix}$

### Equality of two matrices

$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2}$   $B = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2}$

$A = B$

$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2}$   $B = \begin{bmatrix} a & b \\ c & d \end{bmatrix}_{2 \times 2}$

$A = B$

It means  $a=1, b=2$   
 $c=3, d=4$

### Multiplication of two matrices.

• If  $A = [a_{ij}]_{m \times n}$  &  $B = [b_{ij}]_{n \times r}$

• Then only multiplication happens or performed (It means no. of col. of first matrix = No. of row of 2<sup>nd</sup> matrix)  
1<sup>st</sup> matrix = 2<sup>nd</sup> matrix  
column row.

And the multiplied answer is of order  
 $A \times B = [a_{bij}]_{m \times n}$

eg:  $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2}$   $B = \begin{bmatrix} 0 & 1 & 3 \\ 4 & 2 & -1 \end{bmatrix}_{2 \times 3}$

$\rightarrow A \times B = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2} \times \begin{bmatrix} 0 & 1 & 3 \\ 4 & 2 & -1 \end{bmatrix}_{2 \times 3}$

$= \begin{bmatrix} (1 \times 0) + (2 \times 4) & (1 \times 1) + (2 \times 2) & (1 \times 3) + (2 \times (-1)) \\ (3 \times 0) + (4 \times 4) & (3 \times 1) + (4 \times 2) & (3 \times 3) + (4 \times (-1)) \end{bmatrix}$

$= \begin{bmatrix} 0 + 8 & 1 + 4 & 3 - 2 \\ 0 + 16 & 3 + 8 & 9 - 2 \end{bmatrix}$

$= \begin{bmatrix} 8 & 5 & 1 \\ 16 & 11 & 7 \end{bmatrix}$

$$= \begin{bmatrix} 8 & 5 & 1 \\ 16 & 11 & 5 \end{bmatrix} 2 \times 3$$

$$\text{rows } \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \beta$$

$$\text{rows } \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \beta$$